

NAME..... INDEX
NO.....

121/1
MATHEMATICS ALT A
PAPER 1
SEPTEMBER, 2022
TIME: 2½ HOURS

ADM NO.....

CLASS.....

LANJET JOINT EXAMINATION - 2022

Kenya Certificate of Secondary Education

MATHEMATICS ALT A
PAPER 1
TIME: 2½ HOURS

INSTRUCTION TO CANDIDATE'S:

- (a) Write your name, index number and school in the spaces provided at the top of this page.
- (b) Sign and write the date of examination in spaces provided above.
- (c) This paper consists of **TWO** sections: **Section I** and **Section II**.
- (d) Answer **ALL** the questions in **Section I** and any **five** questions from **Section II**.
- (e) **Show all the steps in your calculation, giving your answer at each stage in the spaces provided below each question.**
- (f) Marks may be given for correct working even if the answer is wrong.
- (g) **Non-programmable** silent electronic calculators and **KNEC** Mathematical tables may be used, except where stated otherwise.
- (h) **This paper consists of 16 printed pages.**
- (i) **Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.**
- (j) **Candidates should answer the questions in English.**

FOR EXAMINER'S USE ONLY:

SECTION I

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	TOTAL

SECTION II

17	18	19	20	21	22	23	24	TOTAL

Grand
Total

--

SECTION I: (50 MARKS)

Answer all the questions in this section in the spaces provided.

1. Two signals have been set to flash at interval of 15 minutes, 24 minutes if they flash at 8.13am
When will they flash together again? (2 marks)

2. Solve for m in the equation: (3 marks)
 $3^{4(m+1)} + 3^{4m} = 246$

3. Use tables of cubes, cube roots and reciprocals to find the value of;

$$\frac{4}{(8.63)^3} + \left(\frac{5}{34.46}\right)^{\frac{1}{3}}$$

4. Evaluate: (3 marks)

$$\frac{\frac{1}{2} \text{ of } 3\frac{1}{2} + 1\frac{1}{2} \left(2\frac{1}{2} - \frac{2}{3} \right)}{\frac{3}{4} \text{ of } 2\frac{1}{2} \div \frac{1}{2}}$$

5. If $\tan X = \frac{4}{3}$, find the value of $\sin^2 X + \cos X$ without using tables or calculator. (3marks)

6. Triangle $A^1B^1C^1$ is the image of triangle ABC under the transformation represented by the matrix $\begin{pmatrix} 3 & 1 \\ 5 & 4 \end{pmatrix}$.
If the area of triangle $A^1B^1C^1$ is 140cm^2 , find the area of triangle ABC. (3 marks)

7. Use the exchange rates below to answer this question

	Buying	selling
1 US dollar	63.00	63.20
1 UK£	125.30	125.95

A tourist arriving in Kenya from Britain had 9600 UK sterling pounds (£). He converted the pounds to Kenya shillings at a commission of 5%. While in Kenya he spent $\frac{3}{4}$ of this money. He changed the balance to US dollars after his stay. If he was not charged any commission for this last transaction, calculate to the nearest US dollars the amount he received. (3mks)

8. Convert $0.\dot{1}2\dot{3}$ into a fraction. (3 marks)

9. A train moving at an average speed of 72km/hr. takes 15 seconds to complete cross a bridge that is 80m long. Find the length of the train. (3 marks)

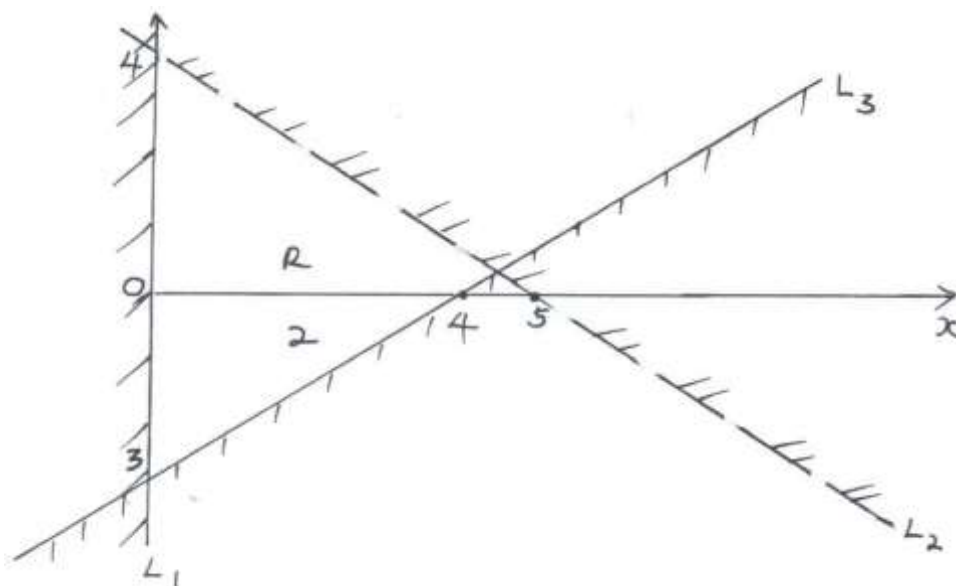
10. The interior angle of a regular polygon is $6\frac{1}{2}$ times the exterior angle. How many sides does the polygon have? (3 marks)

11. Simplify:
$$\frac{3a^2 - 48}{48 - 24a + 3a^2}$$
 (3 marks)

12. A solid metal cuboid 1.5m long, 0.4m wide and 0.25m high is made of material of density 7.5g/cm^3 . Calculate its mass in kg. (3 marks)
13. Find the equation of a straight line which is equidistant from the points A (2, 3) and B (6, 1). Express your answer in the form $\frac{x}{a} + \frac{y}{b} = 1$ where a and b are constant. (3marks)
14. Ruto is $2\frac{1}{4}$ times as old as his son. Five years ago, the ratio of their ages was 8:3. What will be their ages 6 years from now? (4 marks)

15. Two similar cylinders have diameter of 7cm and 21cm. If the larger cylinder has a mass of 6237g. Find the mass of the smaller cylinders. (4 marks)

16. Find the inequalities that define the region R shown in the figure below. (3 marks)



SECTION B: (50 MARKS)

Answer any FIVE questions from this section.

17. Samatha and Meshi entered into a business partnership in which they contributed Kshs. 120,000 and Kshs. 150,000 every year respectively. After one year Fuki joined the business and contributed Kshs. 90,000

a) Calculate the ratio of their investment after 3 years of business (3mks)

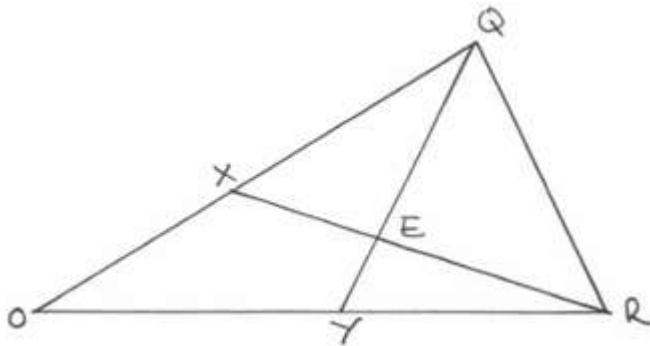
b) It was agreed that 30% of the profits after 3 years be used to cater for the cost of running the business, while the remaining would be shared proportionally. Calculate each person's share if

the profit made after three years was Kshs, 187,000.

(4mks)

- c) If each of them invested their shares in the business, find their new individual investments at the beginning of the fourth year. (3mks)

18. In the figure below $OQ = q$ and $OR = r$. Point X divides OQ in the ratio 1:2 and Y divides OR in the ratio 3:4. Lines XR and YQ intersect at E .



- (a) Express in terms of q and r .
(i) XR . (1 mark)

(ii) YQ. (1 mark)

(b) If $\vec{XE} = m\vec{XR}$ and $\vec{YE} = n\vec{YQ}$, express \vec{OE} in terms of
(i) r, q and m. (1 mark)

(ii) r, q and n. (1 mark)

(c) Using the results in (b) above, find the values of m and n. (6 marks)

19. A car accelerates from rest for 10seconds until it reaches a velocity of 12meters per second. It then continues at this velocity for the next 40 seconds after which it breaks are applied and it comes to rest at a constant retardation of 1.5meters per second squared.

a) Determine

i) The acceleration over the first 10seconds (2mks)

ii) The time taken during the retardation (2mks)

b) Draw the velocity time graph for the journey and use it to determine

i) The total distance covered by the car (4mks)

ii) The percentage of the total distance which was covered during the first 15 seconds. (2mks)

20. (a) Complete the table given below for the equation $y = -2x^2 + 3x + 3$ for the range $-2 \leq x \leq 3.5$ by filling in the blank spaces. (2 marks)

x	-2	-1.5	-1	-0.5	0	0.5	1	1.5	2	2.5	3	3.5
y		-6		1						-2		-11

(b) Use the values from the table above to draw the graph of $y = -2x^2 + 3x + 3$. (3 marks)

(c) Use your graph to:

(i) determine the integral values of χ in the graphs range which satisfy the inequality $2\chi^2 - 3\chi - 3 \geq 3$. (3 marks)

(ii) Solve $-2\chi^2 + 2\chi + 5 = 0$. (2 marks)

21. A sector of a circle of radius 40cm subtends an angle of 26° at the centre of the circle.

$\left(\text{Take } \pi = \frac{22}{7} \right)$.

(a) Calculate

- (i) The area of the sector. (2 marks)
- (ii) The length of the arc. (2 marks)
- (b) The sector is folded to form an inverted right cone. Calculate
- (i) The base radius of the cone. (2 marks)
- (ii) To one decimal place, the vertical height of the cone. (2 marks)
- (c) Calculate the capacity of the cone in litres. (2 marks)

22. The table below shows marks obtained by 100 candidates at Eastside High School in a Biology examination.

Marks	15 - 24	25 - 34	35 - 44	45 - 54	55 - 64	65 - 74	75 - 84	85 - 94
Frequency	6	14	24	14	χ	10	6	4

- (a) Determine the value of χ . (2 marks)

- (b) State the modal frequency. (1 mark)

- (c) Calculate the median mark. (4 marks)

- (d) Calculate the mean mark. (3 marks)

23. A straight line passes through points (8, -2) and (4, -4)

a) Write its equation in the form $ax + by + c = 0$ where a, b and c are integers. (3 marks)

b) If the line in (a) above cuts the x axis at point P, determine the coordinates of P. (2 marks)

c) Another line which is perpendicular to the line in (a) above passes through point P and cuts the Y axis at the point Q. Determine the co-ordinates of point Q. (3 marks)

d) Find the length of QP. (2 marks)

24. (a) After t seconds, a particle moving along a straight line has a velocity of V m/s and an acceleration of $(5 - 2t)$ m/s². The particles initial velocity is 2m/s.
- (i) Express V in terms of t . (3 marks)
- (ii) Determine the velocity of the particle at the beginning of the third second. (2 marks)
- (b) Find the time taken by the particle to attain maximum velocity and the distance it covered to attain the maximum velocity. (5 marks)